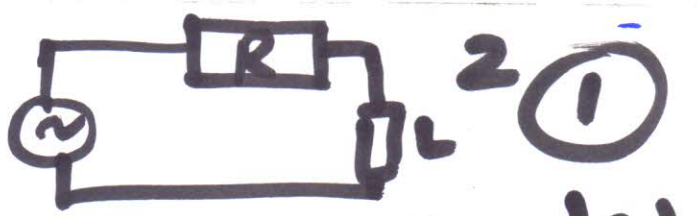


① Energy source



" provide the Voltage needed to force Current (electrons) through circuit."

② Conductors

" Through which the current can travel"

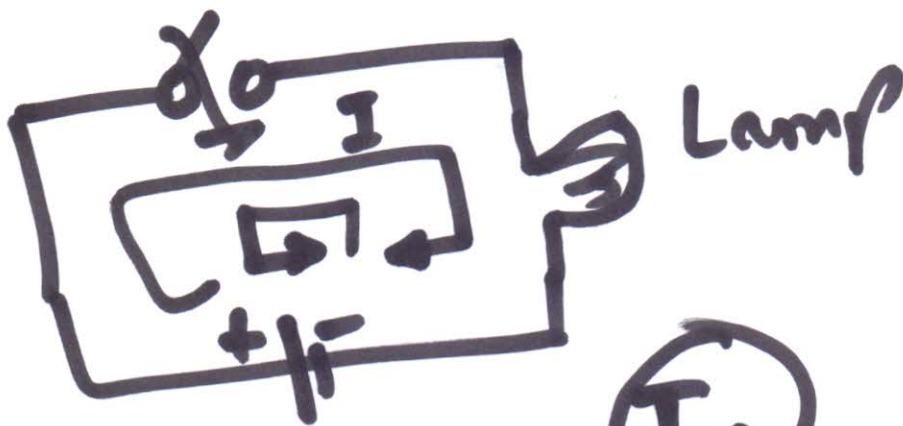
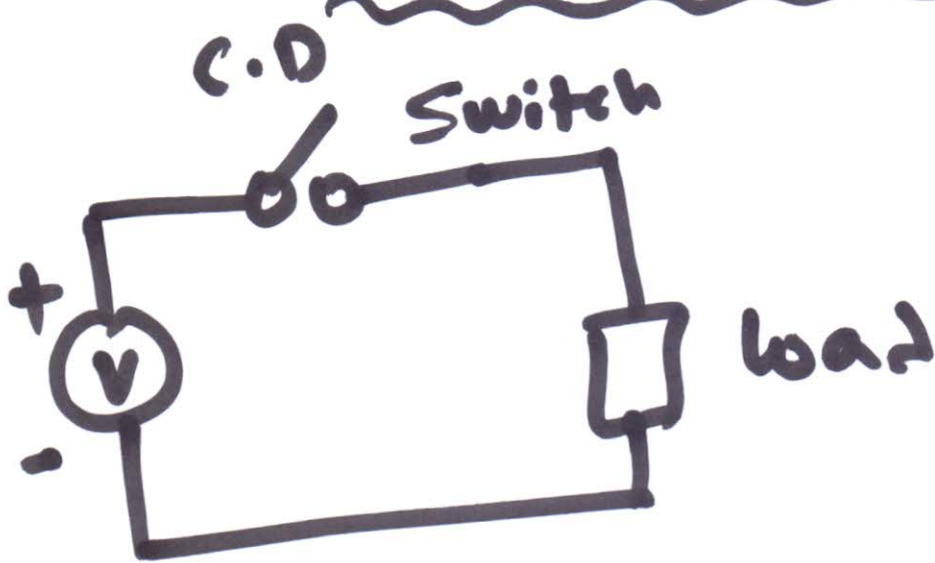
③ Insulators

" Confine the Current and convert the EE taken from the Energy source."

④ Control device, " often a switch, to start/stop the flow of I.

⑤ Protection device, " To interrupt the circuit in case of circuit malfunctions"

# Simple circuit

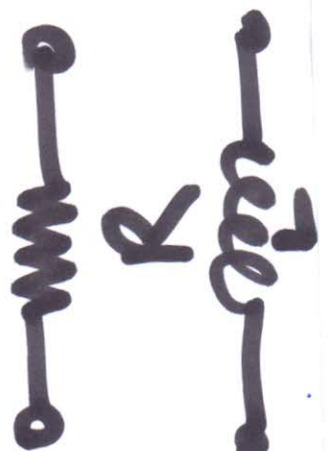


C.D.C

E.F.D.C



Capacitor



Resistor

Inductor

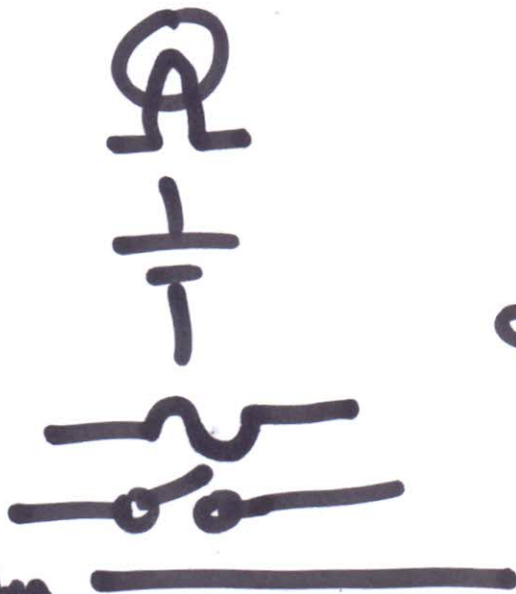
## Symbol

Bulb.

cell

Fuse  
switch

wire/Conductor





# Ampere: (A)

"It is the constant current which when maintained in two // straight conductors of length  $l$  and negligible  $\phi$ -section separated by a distance of one meter in vacuum, produced between these conductors a force equal to  $2 \times 10^{-7}$  Newtons/meter length."

# Coulomb (C).

~~It is the quantity of Electricity conveyed by a current of one Amp flowing through a solid conductor at constant temperature is proportional to~~

## Coulomb (Q)

2(4)

$$Q = It, \quad I = Q/t$$

$$1 \text{ Coulomb} = 1 \text{ Ampere-second}$$

$$1 \text{ Amp} = 1 \text{ Coulomb/sec}$$

Quantity of electricity conveyed by a current of one ampere flowing for one second

$$\text{ampere-hour} = \text{Ah}$$

$$1 \text{ amp-hour} = 3600 \text{ Coulombs}$$

## Difference of Potential (V)

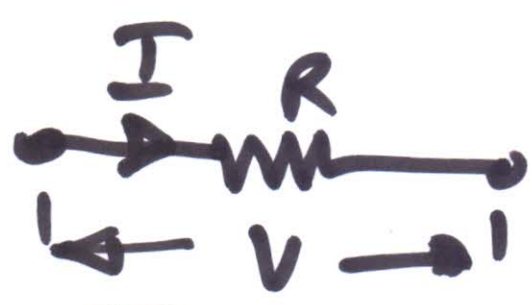
Voltage / Electrical pressure required to drive the current between them is called Difference of Potential.



# Ohm's Law

The relationship between current (I), Voltage (V) and resistance (R) was discovered by a German Scientist named, Georg Ohm. This relationship is named Ohm's Law in his honor.

Ohm found that the current in a circuit varies directly with the voltage when the resistance is kept constant



$$I \propto V \quad (R - \text{Constant})$$

# Ohm's Law States

⑥

"The Current is directly proportional to the Voltage and Inversely proportional to the resistance."

(R - Const.)

$$I \propto V$$

$$I \propto \frac{1}{R}$$

$$I = V/R \times \text{Constant}$$

$$\boxed{V = IR}$$

V = Volts

R = Ohms

I = Amperes.

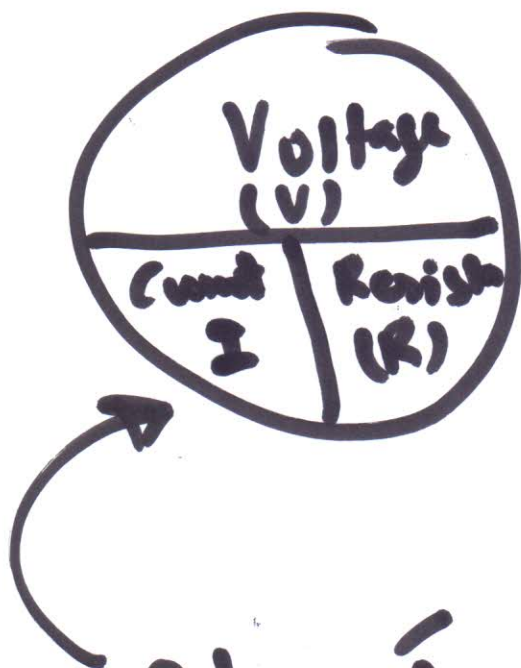
Constant = 1

Ohm's Law equation

$$\boxed{I = V/R}$$



⑦



$$V = IR$$

$$I = \frac{V}{R}$$

$$R = \frac{V}{I}$$

Ohm's Law circle

Unit of Potential Difference (P.D)  
and Electromotive Force (e.m.f)

e.m.f / P.D  $\Rightarrow$  Volt.

1 Volt = 1 joule / Coulomb

The P.D between two points is one Volt if one joule of energy is used in sending one Coulomb between them.

The Volt is therefore defined as the P.D across a resistance of one Ohm carrying a current of one Ampere.

$$\text{Current} = \frac{\text{P.D}}{\text{Resistance}} = \frac{V}{R} \text{ (8)}$$

$$\text{P.D} = \text{Current} \times \text{Resistance} = IR$$

$$\text{Resistance} = \frac{\text{P.D}}{\text{Current}} = \frac{V}{I}$$

---

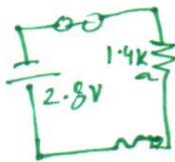
V - Volt - KV - MV, mV

I = Ampere = A - kA -

R = ohm =  $\Omega$ , - k $\Omega$ , - M $\Omega$  - m $\Omega$

---

Example: 3.1



$$V = 2.8 \text{ Volts}$$

$$R = 1.4 \text{ k}\Omega$$

$$I = \frac{V}{R} = \frac{2.8}{1400}$$

$$I = 0.002 \text{ A}$$

Exp. 3.2

$$R = 96 \Omega$$

$$V = 120 \text{ V}$$

$$I = \frac{120}{96} = 1.25 \text{ A}$$

$$I = 1.25 \text{ A}$$



Do yourself - 3.3, 3.4, 3.5.

2(9)

Power = Current (I) × Voltage (V)

$$P = IV = I^2 R = \frac{V^2}{R}$$

P = Watts, if V = Volts, I = Amperes.

---

Exp 3.6

Current (I) = 3 A

Voltage (V) = 120 V

Power (P) = VI.

$$= 3 \times 120$$

$$= 360 \text{ (Watts)}$$

---

Exp 3.7

$$V = 120 \text{ V}$$

$$P = 500 \text{ W}$$

$$I = \frac{P}{V} = \frac{500 \text{ W}}{120 \text{ V}} = 4.17 \text{ A}$$

Do Exp 3.8, ... 3.13

## Calculating cost.

The cost of E.E can be determined from the amount of energy used and the cost rate.

The cost rate is usually specified in Rs: per Kilowatt hour.

The cost of Electric Energy is:

$$\text{Cost} = \text{Rate} \times \text{Energy}$$

$$= \text{Rupees per Kilowatt hour} \times \text{Kilowatt hours}$$

Exp: 3.14: Energy cost = ?

$$\text{Energy} = 120 \text{ kWh}$$

$$\text{Rate} = \text{Rs: } 6/\text{kWh}$$

$$\text{Cost} = 6 \times 120 = 720 \text{ Rupees.}$$



## Exp: 3.15

2 (11)

$$P = 100 \text{ W (Lamp)}$$

$$t = 3 \text{ h}$$

$$\text{Rate} = \text{Rs: } 6/\text{kWh}$$

Q = Cost of operating lamp  
for 3-hours:

Sol:

$$P = 100 \text{ W}$$

$$t = 3 \text{ h}$$

$$\text{Cost} = \text{Rate} \times \text{energy}$$

$$\text{Energy} = P \times t$$

$$= 100 \times 3$$

$$= 300 \text{ Wh}$$

$$= 0.3 \text{ kWh}$$

$$\text{Cost} = 0.3 \times 6$$

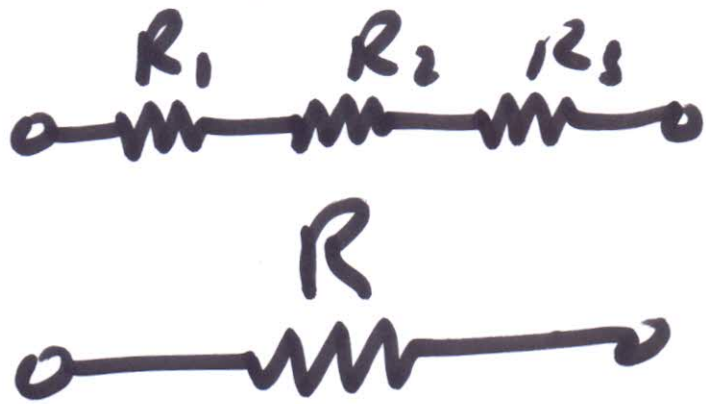
$$= \text{Rs: } 1.8$$

Solve:  
3.16.

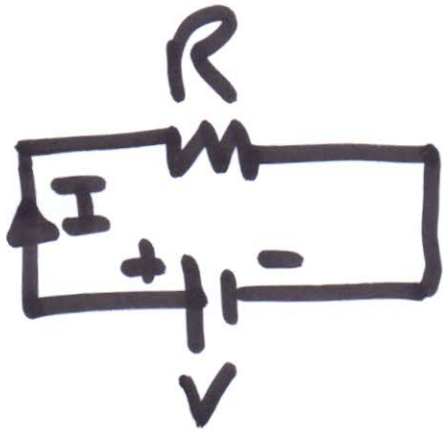
# Arrangement of Resistors

2 (12)

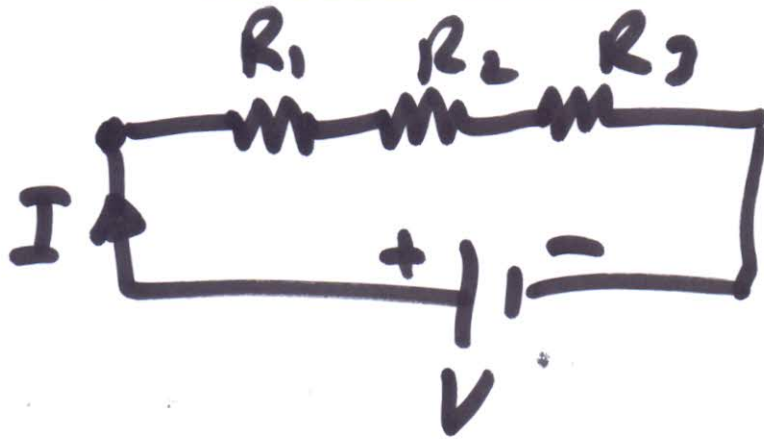
Series Arrangement



$$R = R_1 + R_2 + R_3$$



$$V = IR$$

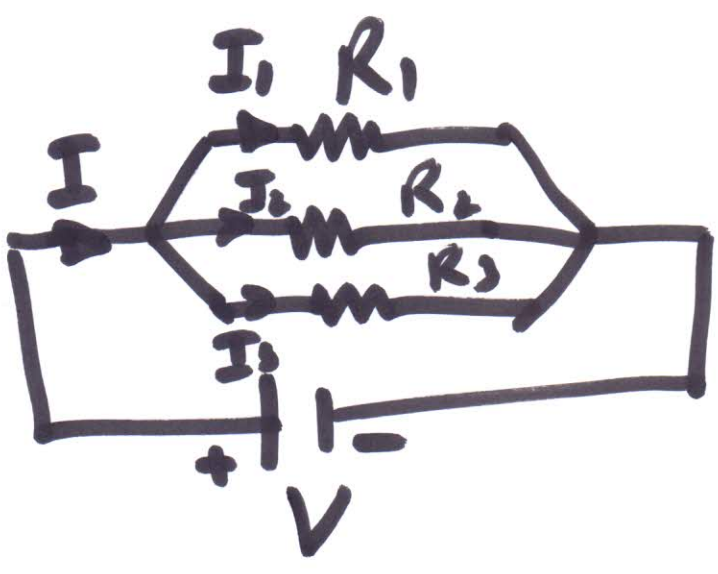
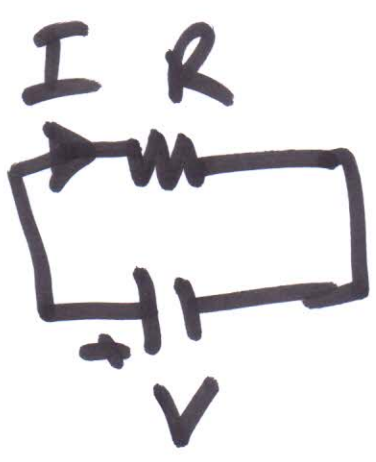


$$V = IR_1 + IR_2 + IR_3$$

$$IR = I(R_1 + R_2 + R_3)$$

$$R = R_1 + R_2 + R_3$$





$$I = \frac{V}{R}$$

$$I_1 = \frac{V}{R_1}, I_2 = \frac{V}{R_2}, I_3 = \frac{V}{R_3}$$

$$I = \frac{V}{R}$$

$$I = I_1 + I_2 + I_3$$

$$\frac{V}{R} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

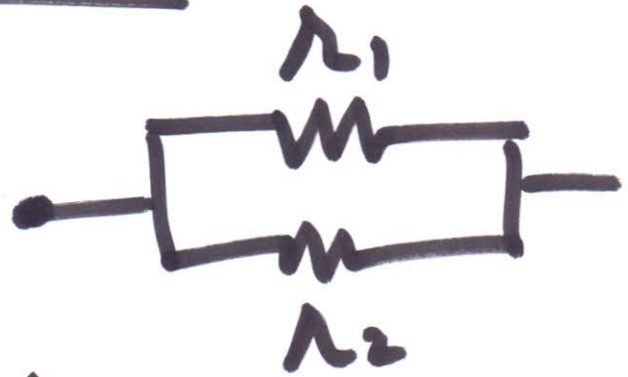
$$R = \frac{1}{3} R_0$$

$$R_1 = R_2 = R_3 = R_0$$

$$\frac{1}{R} = 3 \frac{1}{R_0}$$

## Two Equal Resistors

2 (14)

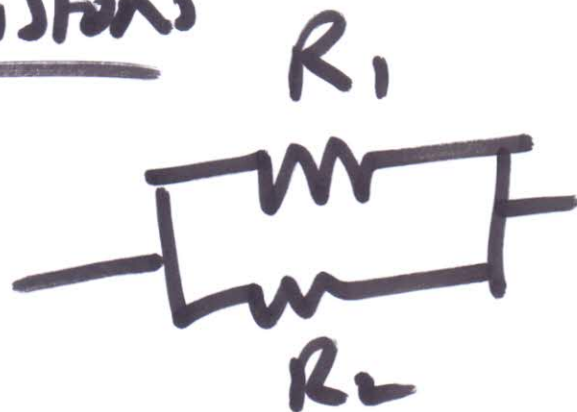


$$R_1 = R_2 = R$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} = \frac{1}{R} + \frac{1}{R}$$

$$R_{eq} = \frac{R}{2}$$

## Unequal Resistors



$$\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

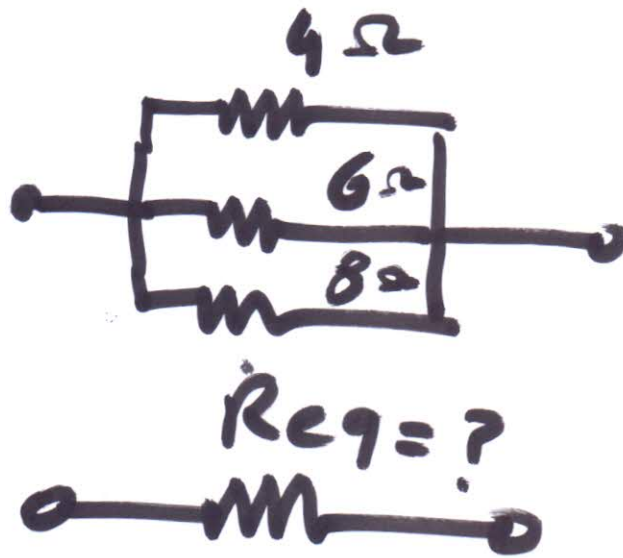
$$\frac{1}{R} = \frac{R_1 + R_2}{R_1 R_2}$$

$$R = \frac{R_1 \cdot R_2}{R_1 + R_2}$$



## Example: A

② (15)

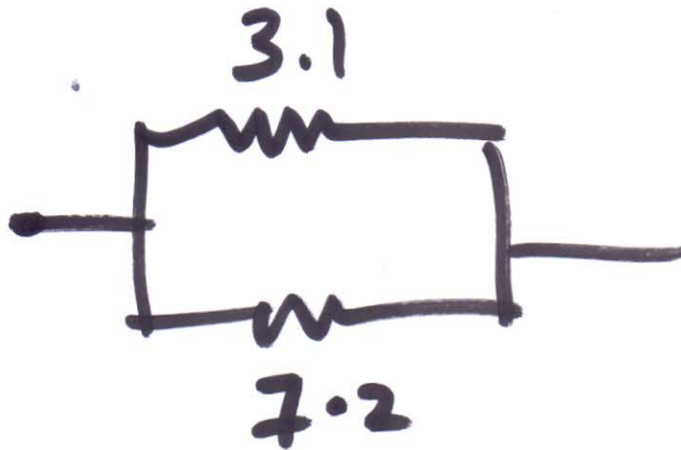


$$\frac{1}{R} = \frac{1}{4} + \frac{1}{6} + \frac{1}{8}$$

$$\frac{1}{R} = \frac{6+4+3}{24} = \frac{13}{24}$$

$$R = \frac{24}{13} = 1.846 \Omega$$

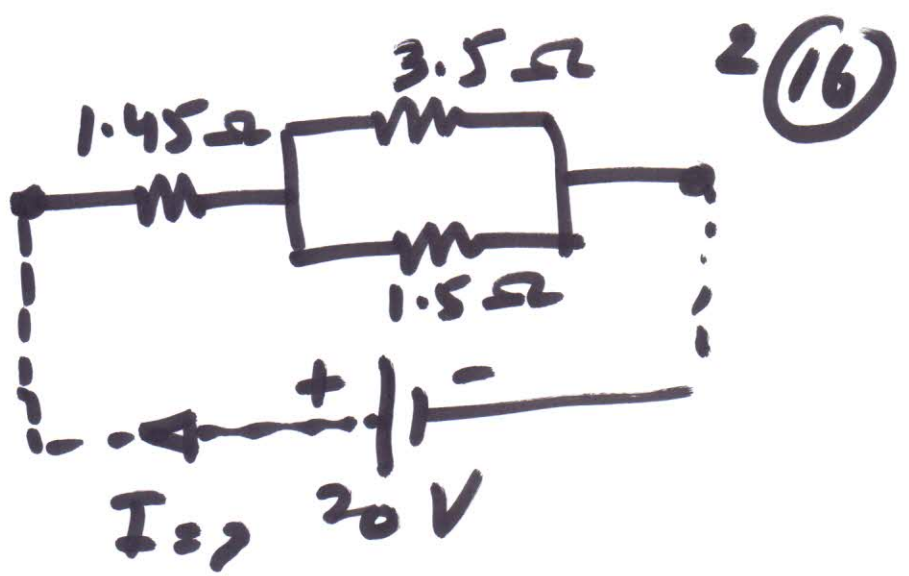
## Example - B



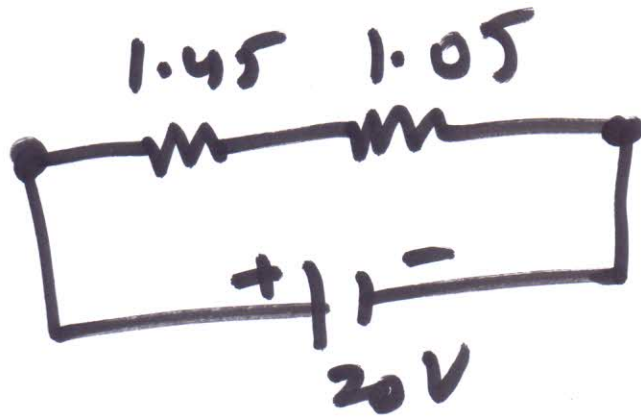
Equivalent Resistor =  $\frac{\text{Product}}{\text{Sum}}$

$$R_{eq} = \frac{3.1 \times 7.2}{3.1 + 7.2} = 2.16 \Omega$$

# Exp. C

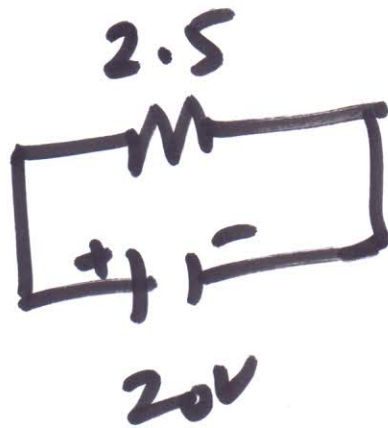


$$\text{Parallel } R_p = \frac{3.5 \times 1.5}{3.5 + 1.5} = 1.05 \Omega$$



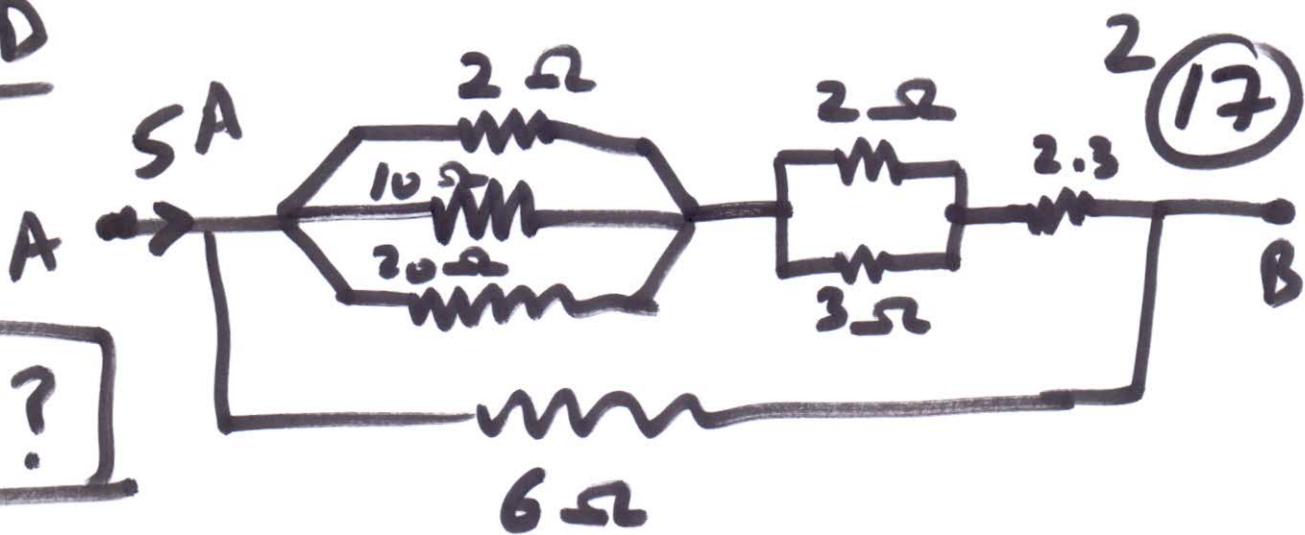
$$R_t = 1.45 + 1.05 \\ = 2.5 \Omega$$

$$I = \frac{20}{2.5} = \frac{V}{R}$$



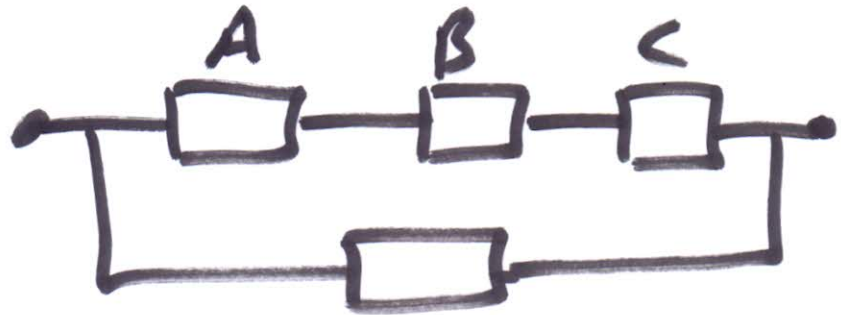
$$I = 8 \text{ Amperes}$$

# Exp-D



$V_{AB} = ?$

$R_{eq} = ?$



$V_{AB} \cdot 5 \times 3 = 15 \text{ Volt}$

$R_A = ?$

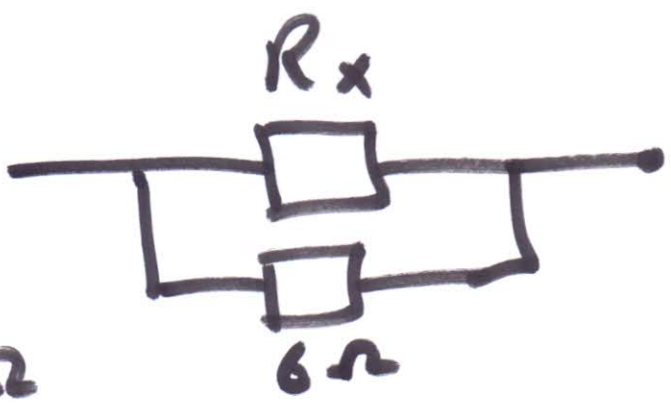
$$\frac{1}{R_A} = \frac{1}{4} + \frac{1}{10} + \frac{1}{20} = \frac{8}{20}$$

$$R_A = 2\frac{1}{2} \Omega$$

$R_B = ?$

$$R_B = \frac{2 \times 3}{2 + 3} = \frac{6}{5} = 1.2 \Omega$$

$R_C = 2.3$



$$R_x = R_A + R_B + R_C$$

$$= 2.5 + 1.2 + 2.3 = 6 \Omega$$

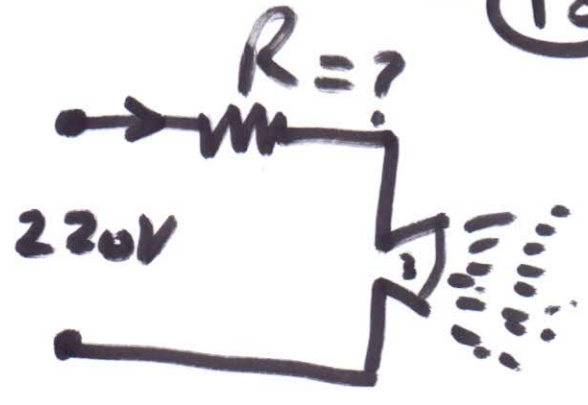
$$R_{eq} = \frac{6 \times 6}{6 + 6} = \frac{36}{12} = 3 \Omega$$





Ex-E

A search light takes 100A at 80V. It is to be operated from 220V supply.



Find the value of  $R = ?$

Ans:

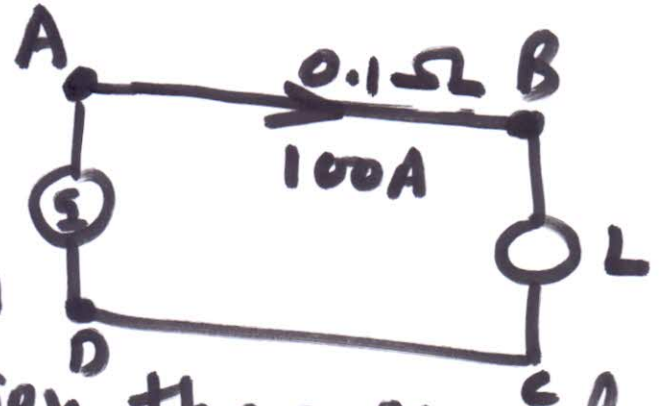
P.d across Bulb is 80V then P.d across  $R = 220 - 80$

$$V_R = 140V$$

$$R = \frac{V}{I} = \frac{140}{100} = 1.4 \Omega$$

P.F

load taking 100A  
110 Volts is supplied



a generating station through a pair of cables each having resistance of  $0.1 \Omega$  at generating station = ?

Loss of Voltage  
due to resistance  
of the cable.

$$V_{AB} = IR = 100 \times 0.1 = 10 \text{ Volt}$$

Similarly

$$V_{CD} = IR = 100 \times 0.1 = 10 \text{ Volt}$$

There is total loss of voltage 20V,  
Called the Volt drop in the Lead.

Voltage at generating

$$\begin{aligned} \text{Station} &= 110 + 20 \\ &= 130 \text{ V} \end{aligned}$$

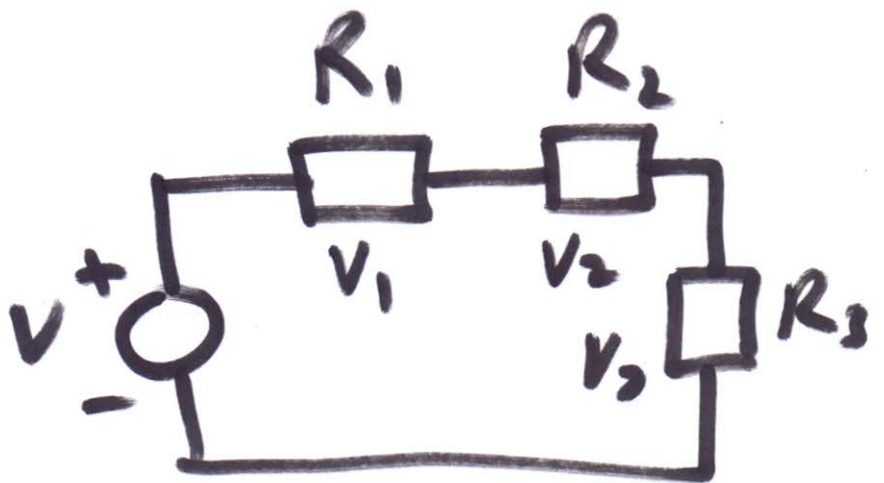
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# Kirchhoff's Law

20

- ① Kirchhoff's Voltage Law (KVL)
- ② Kirchhoff's Current Law (KCL)

## KVL



### Version-1

Sum of the Voltage rises are equal to Sum of Voltage drops in a closed loop:

$$V = V_1 + V_2 + V_3 \rightarrow \textcircled{A}$$

### Version-2

$$\sum V = 0$$

Algebraic Sum of the voltages in a close loop is equal to zero.

Voltage Rise = +ive  
Voltage Drops = -ive

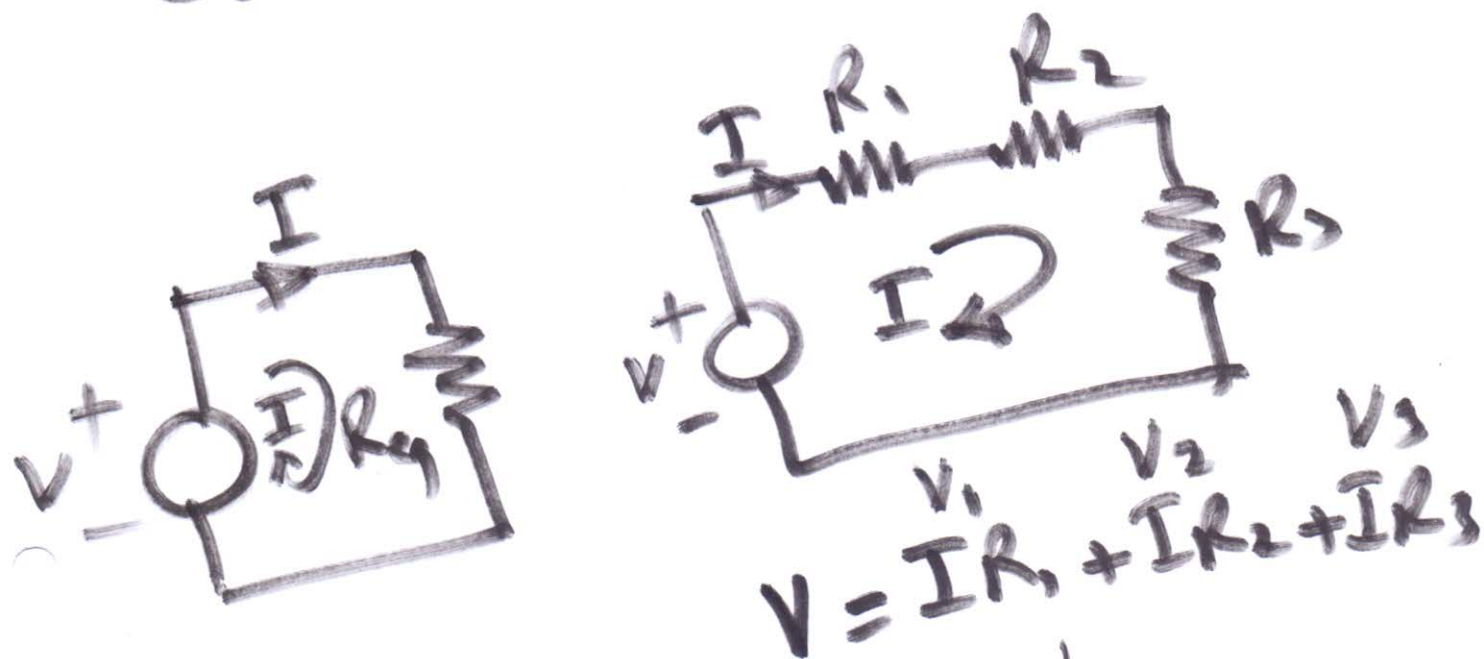


$$V + (-V_1) + (-V_2) + (-V_3) = 0$$

↳ (B)

Equation A is same to Equation B

Series combination of Resistors  
can be proved using KVL.



$$V = IR_1 + IR_2 + IR_3$$

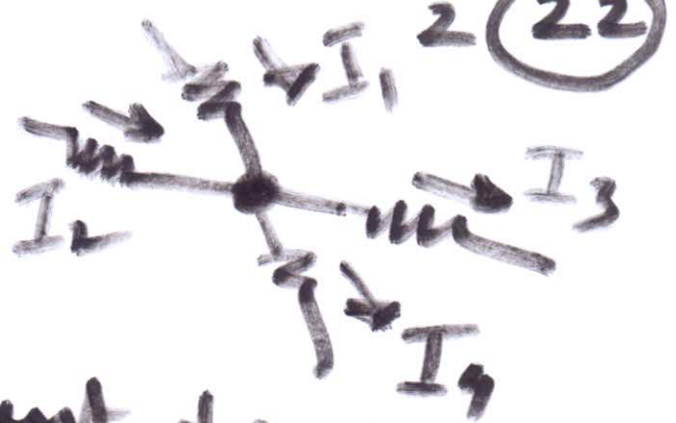
$$V = I \cdot R_{eq}$$

$$I R_{eq} = I (R_1 + R_2 + R_3)$$

$$R_{eq} = R_1 + R_2 + R_3$$

# KCL

## Version-1



Sum of the Current to a node must be equal to sum of the currents going away from the node.

$$I_1 + I_2 = I_3 + I_4 \rightarrow \textcircled{A}$$

## Version-2

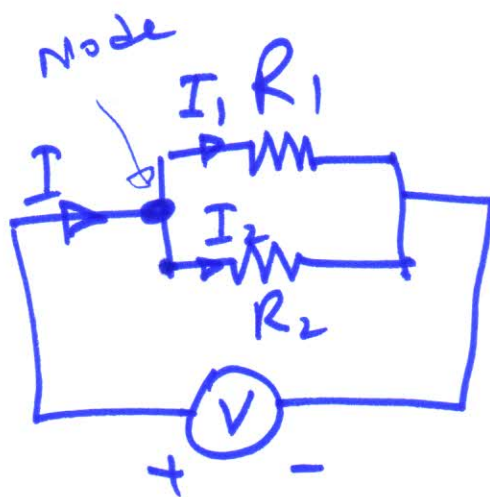
Algebraic Sum of All currents at a node must be equal to zero.

$$\sum I = 0$$

$I \xrightarrow{\text{to}} \text{node} \text{ +ive}$   
 $I \xleftarrow{\text{away}} \text{from node} \text{ -ive}$

$$I_1 + I_2 + (-I_3) + (-I_4) = 0 \rightarrow \textcircled{B}$$

Eq:  $\textcircled{A}$  and  $\textcircled{B}$  are same.



$$V = IR_{eq}$$

According to K.C.L.

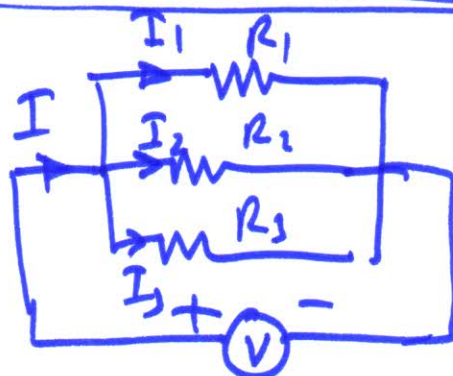
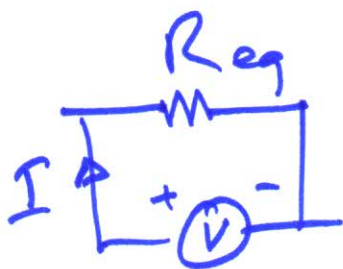
$$I = \frac{V}{R_{eq}}$$

$$I = I_1 + I_2$$

$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2}$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2}$$

$$R_{eq} = \frac{R_1 \cdot R_2}{R_1 + R_2}$$



$$I = \frac{V}{R_{eq}}$$

$$I = I_1 + I_2 + I_3 \quad (\text{KCL})$$

$$\frac{1}{R_{eq}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}$$

$$\frac{V}{R_{eq}} = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

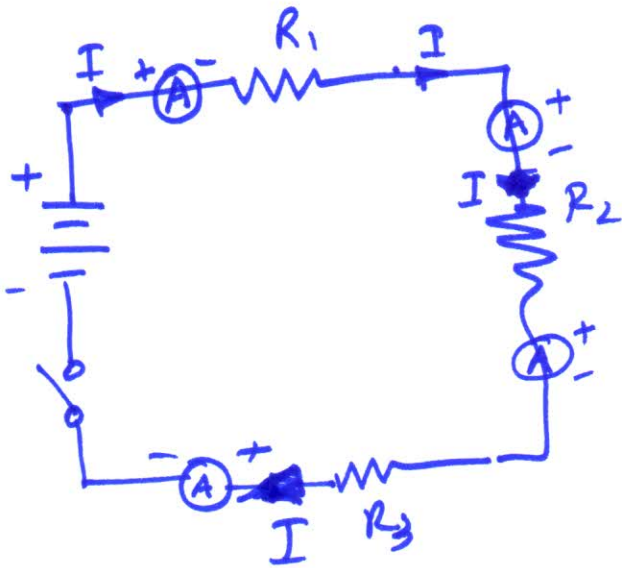


# Ch. 5 Multiple-load circuit

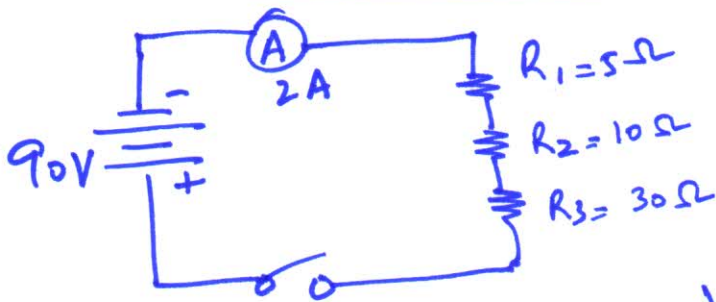
## Series circuits.

Current in series circuits:

Current is same everywhere in series circuit



$$I_T = I_{R_1} = I_{R_2} = I_{R_3}$$



$$R_T = R_1 + R_2 + R_3 = 45\Omega$$

$$R_T = \frac{V}{I} = \frac{90}{2} = 45\Omega$$

## Voltage in Series circuit

The battery voltage in above

circuit divides up across the three load resistors.

It always divides up so that the sum of the individual load voltages equal the source voltage

$$V_T = V_{R_1} + V_{R_2} + V_{R_3} + \dots$$
$$= 10V + 20V + 60V$$


$$V_T = 90V$$

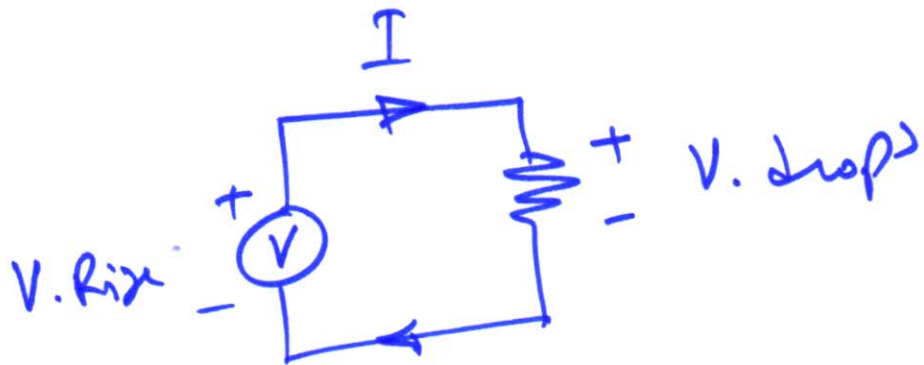
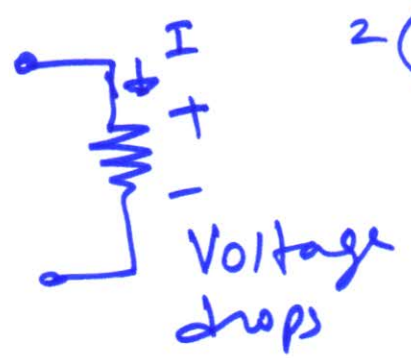
$$V_{R_1} = I_{R_1} \times R_1 = 2A \times 5\Omega = 10V$$
$$V_{R_2} = I_{R_2} \times R_2 = 2A \times 10\Omega = 20V$$
$$V_{R_3} = I_{R_3} \times R_3 = 2A \times 30\Omega = 60V$$

## Voltage drop + Polarity

2 (25)

→ According to conventional Direction of current

 Voltage Rise, Voltage source



$$V_{\text{Rise}} = V_{\text{drop}} = \text{K.V.L.}$$

---

Go through page 102, 103, for open circuit and short circuit

---

Also go through Examples: 5.1, 5.2

---

## Maximum Power Transfer

Maximum power transfer refers to getting max possible amount of power from a source to its load.

The source may be battery, and load a lamp. Or the source could be a guitar amplifier and load a speaker.



Maximum power transfer occurs when the source's internal opposition to the current equals the load's opposition to the current.

Resistance is one form of opposition to current.  
 Impedance is another form of opposition to current.

$R \rightarrow$  in A.C/D.C and  $Z \rightarrow$  in A.C

In d.c circuits, Maximum Power Transfer occurs when resistances are matched.

Example of MPT (Maximum Power Transfer)

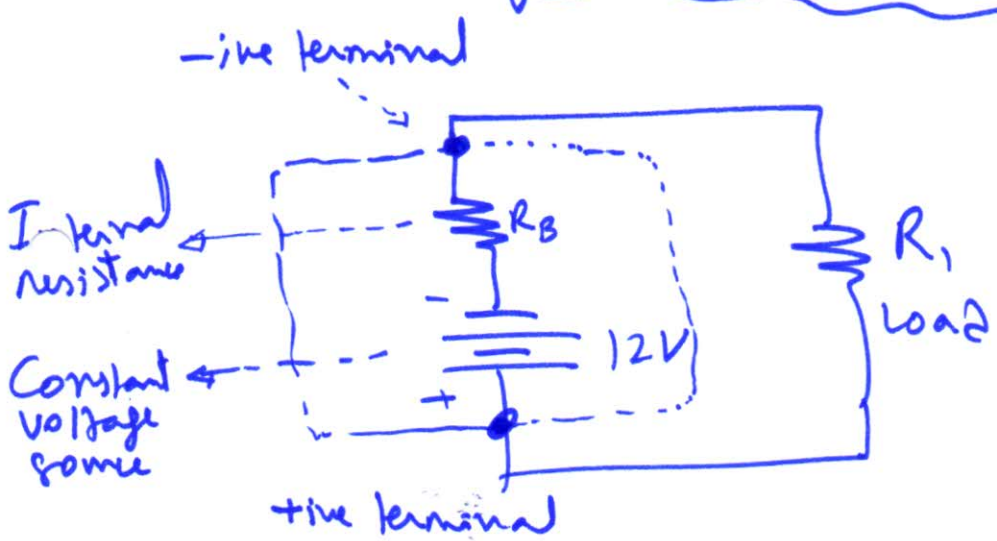


Fig: 5.16  
 Maximum Power Transfer occurs when  $R_B$  and  $R_L$  are equal.

Fix  $R_B = 3$ , Vary  $R_L, 1, 2, 3, 4, \dots, 6$   
 Let us calculate: let  $R_L = 9, R_B = 3$

$R_T = R_L + R_B = 9\Omega + 3\Omega = 12\Omega$

$I_T = \frac{V_T}{R_T} = \frac{12V}{12\Omega} = 1A$

$P_{R_L} = I_T^2 \cdot R_L = (1A)^2 \times 9\Omega = 9W$

$P_{R_B} = I_T^2 \cdot R_B = (1A)^2 \times 3 = 3W$

$P_T = 9W + 3W = 12W$

$R_L$ ( $\Omega$ )	$R_T$ ( $\Omega$ )	$I_T$ A	$P_{R_L}$ W	$P_{R_B}$ W	$P_T$ W
1	4	3.0	9.0	27.0	36
2	5	2.4	11.52	17.28	28
3	6	2.0	12.0	12.0	24
4	7	1.71	11.76	8.82	20
5	8	1.50	11.25	6.75	18
6	9	1.33	10.67	5.33	16



Notice that the maximum power dissipation occurs when  $R_1 = 3\Omega$ .

From the table:

→ We will observe the power dissipated within the source and the total power taken from the source.

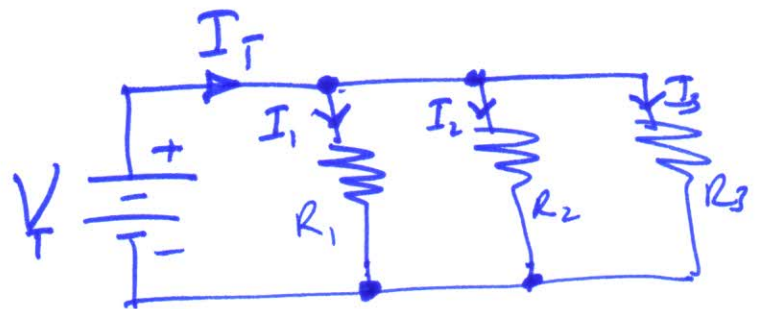
→ <sup>when</sup> Maximum power transfer occurs, the efficiency is only 50%.

→ Of the 24W furnished by source only 12W is used by the load.

→ As the load gets larger, the efficiency improves and the power transferred decreases.

## Parallel circuits

- Same Voltage
- Different Currents



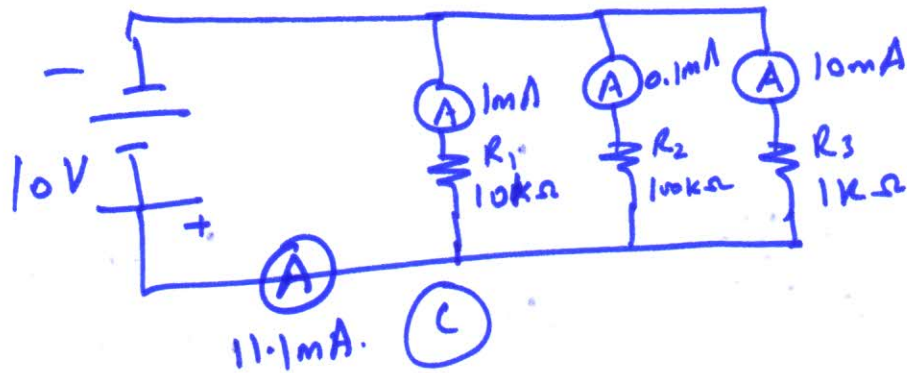
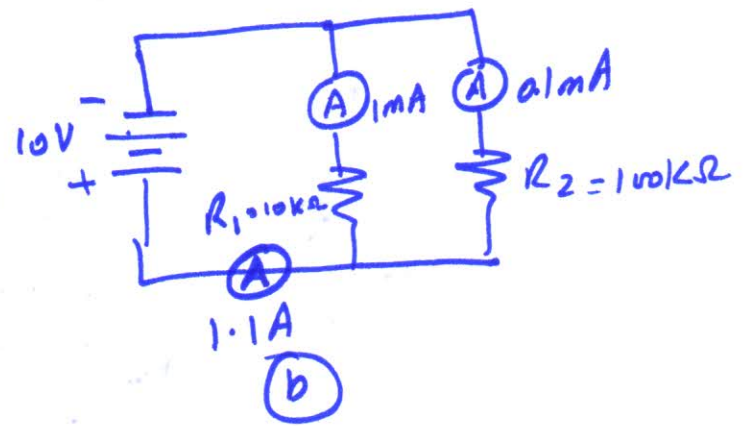
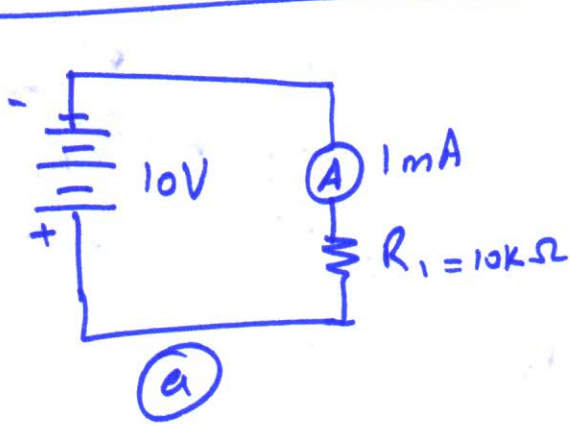
$$V_T = V_{R_1} = V_{R_2} = V_{R_3} = \dots$$

$$I_T = I_1 + I_2 + I_3$$

$$I_T = \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}$$

# Resistance in parallel

(2) (28)



→ Total resistance in parallel circuits.  
Adding resistors in parallel increases total current and decreases total resistance.

$$I_{R_1} = \frac{V}{R_1} = \frac{10V}{10,000} = 0.001A = 1mA$$

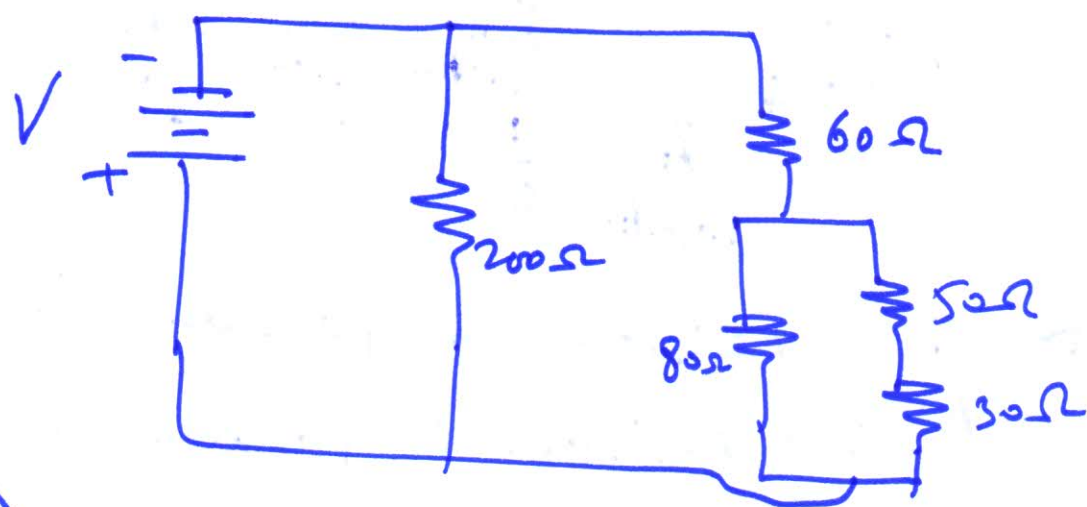
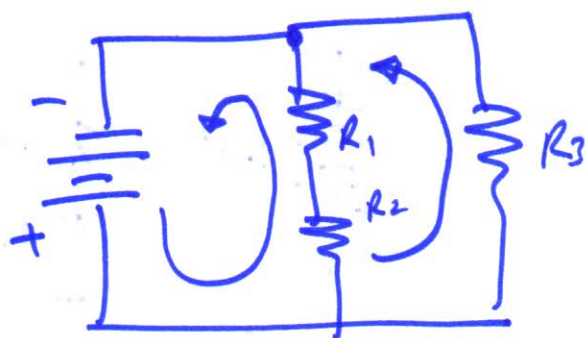
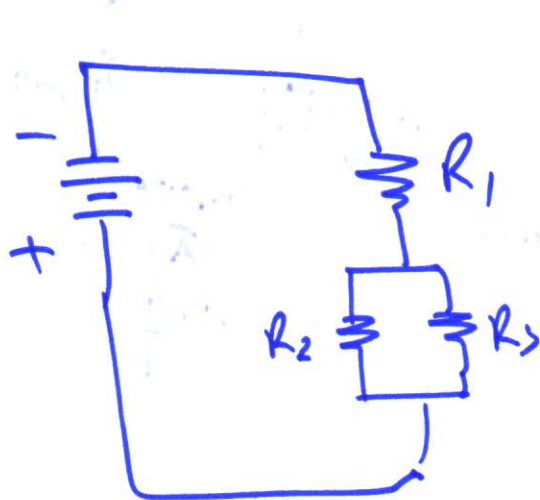
$$I_{R_2} = \frac{V_2}{R_2} = \frac{10V}{100,000\Omega} = 0.0001A = 0.1mA$$

$$I_{R_3} = \frac{10V}{1,000\Omega} = 0.01A = 10mA$$

Solve Example, 5.3, 5.4, 5.5, 5.6

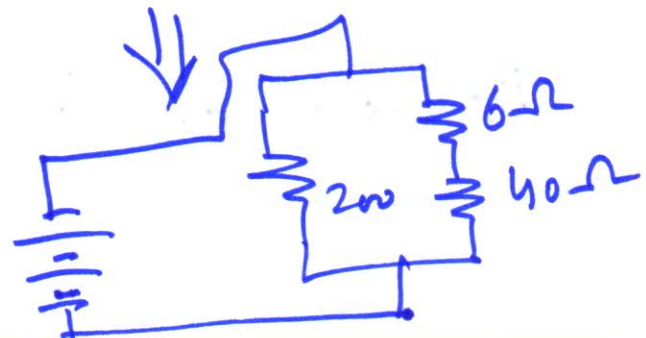
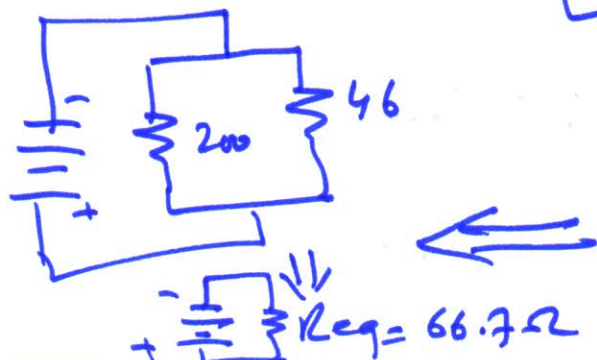
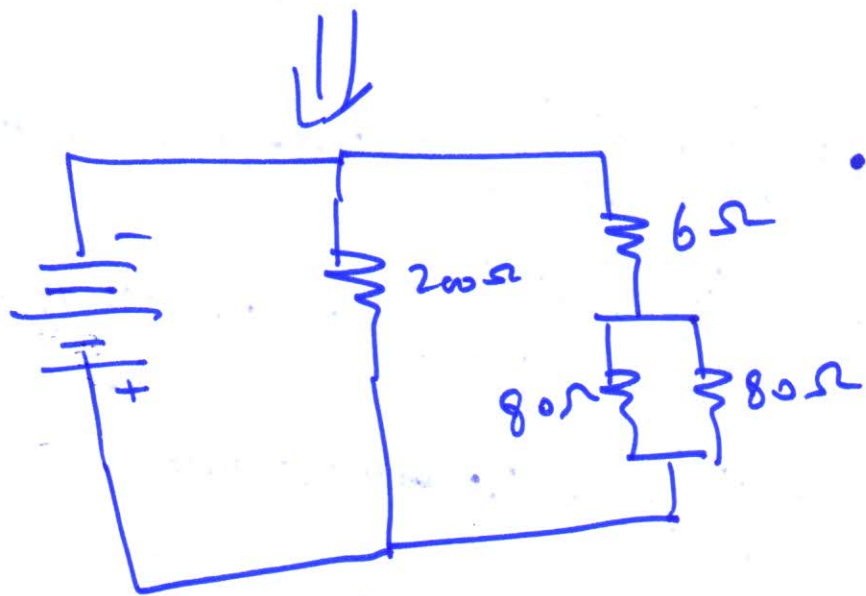
(P.T.O)

# Series Parallel Circuit



Note.

Solve example:  
5.10, 5.11



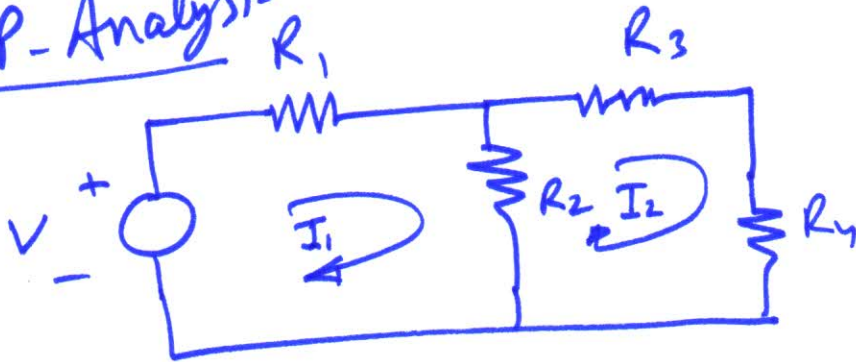


# Further Application of Kirchhoff's Laws

KVL - Loop Analysis/Mesh Analysis

KCL - Node Analysis.

## Loop-Analysis



### Loop-I.

Voltage rises = Voltage drops

$$V = I_1 R_1 + (I_1 - I_2) R_2$$

$$V = I_1 (R_1 + R_2) + I_2 (-R_2) \rightarrow \textcircled{1}$$

### Loop-II

$$0 = I_2 R_3 + I_2 R_4 + (I_2 - I_1) R_2$$

$$0 = I_1 (-R_2) + I_2 (R_2 + R_3 + R_4) \rightarrow \textcircled{2}$$

$$\begin{bmatrix} (R_1 + R_2) & (-R_2) \\ (-R_2) & (R_2 + R_3 + R_4) \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} V \\ 0 \end{bmatrix}$$

General equation

$$\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} I_1 \\ I_2 \end{bmatrix} = \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

Cramer's Rule

$$\Delta_R I = V$$

(2) (30)

$$\text{Solution } I_1 = \frac{\begin{vmatrix} V_1 & R_{12} \\ V_2 & R_{22} \end{vmatrix}}{\Delta_R}$$

$$I_2 = \frac{\begin{vmatrix} R_{11} & V_1 \\ R_{21} & V_2 \end{vmatrix}}{\Delta_R}$$

$$\Delta = \begin{vmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{vmatrix} = R_{11}R_{22} - R_{12}R_{21}$$

1)  $R_{11}$  = Sum of All Resistance in Loop 1

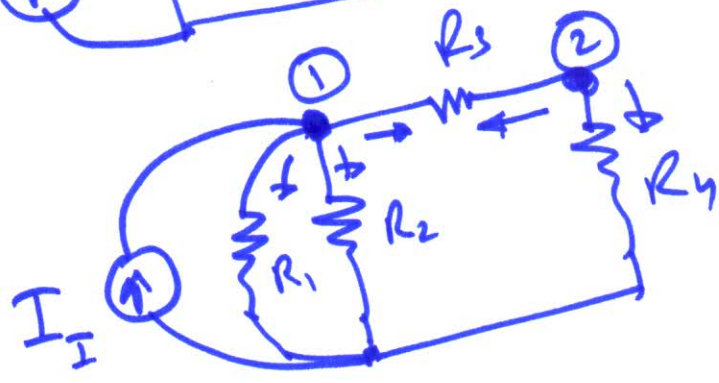
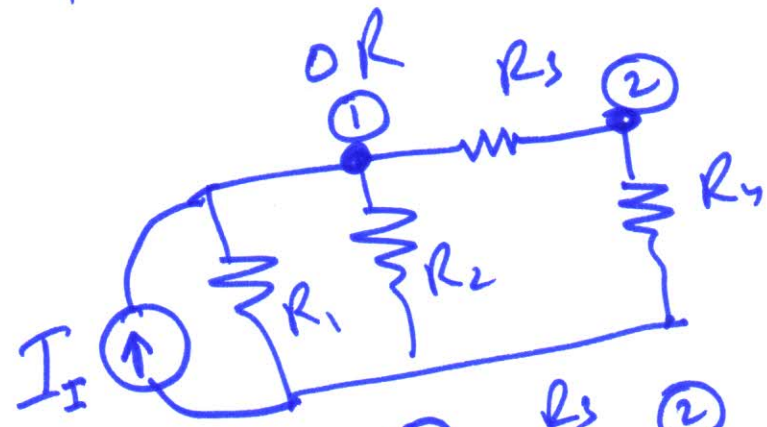
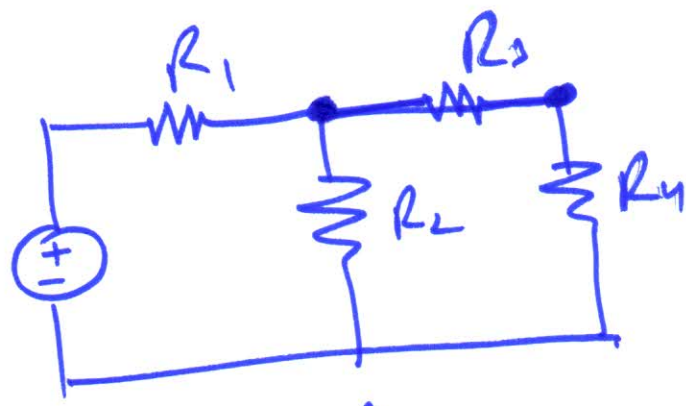
2)  $R_{22}$  = Sum of All Resistance in Loop 2

3)  $R_{12} = R_{21}$  = Resistance Common between Loop 1 and Loop 2.

$V_1$  = Sum of the Voltage rises in Loop-1

$V_2$  = Sum of the Voltage rises in Loop-2.

# Node Analysis



K.C.L

$$I_I = \frac{V_1}{R_1} + \frac{V_1}{R_2} + \frac{V_1 - V_2}{R_3}$$

Node ①  
① ←

$$I_I = V_1 \left( \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3} \right) + V_2 \left( -\frac{1}{R_3} \right)$$

$$0 = \frac{V_2 - V_1}{R_3} + \frac{V_2}{R_4}$$

$$0 = V_1 \left( -\frac{1}{R_3} \right) + V_2 \left( \frac{1}{R_4} + \frac{1}{R_3} \right)$$



$$\begin{bmatrix} \left(\frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}\right) & \left(-\frac{1}{R_3}\right) \\ \left(-\frac{1}{R_3}\right) & \left(\frac{1}{R_3} + \frac{1}{R_4}\right) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ 0 \end{bmatrix}$$

$$\frac{1}{R} = G$$

$$\begin{bmatrix} (G_1 + G_2 + G_3) & (-G_3) \\ (-G_3) & (G_3 + G_4) \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ 0 \end{bmatrix}$$

Generalized Equation:  $\begin{bmatrix} G_{11} & G_{12} \\ G_{21} & G_{22} \end{bmatrix} \begin{bmatrix} V_1 \\ V_2 \end{bmatrix} = \begin{bmatrix} I_1 \\ I_2 \end{bmatrix}$

⊕  $G_{11}$  = Sum of all conductance connected to node-1

⊕  $G_{22}$  = Sum of all conductance connected to node-2

⊖  $G_{12} = G_{21}$  = Conductance common between node-1 and node-2

⊕ if towards node-1  $-I_1 =$  Current source connected to node-1 (2) (33)

⊕ if towards node-2  $I_2 =$  Current source connected to node-2

and (-ive) if away from the node - (2)

$$[G][V] = [I]$$

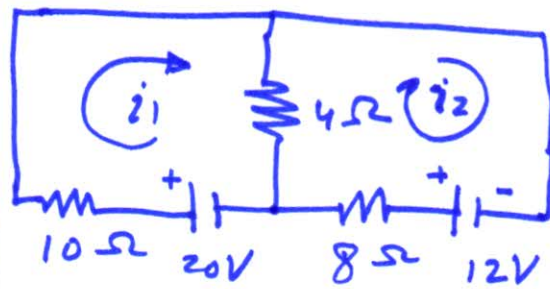
Solution is Cramer's rules or Straight method.

Chapter VIII  
Admissibility.

Kirchhoff's Law

Exp. 1 (Page-64)

$$\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 20 \\ 12 \end{bmatrix}$$



$$R_{11} = 10 + 4 = 14$$

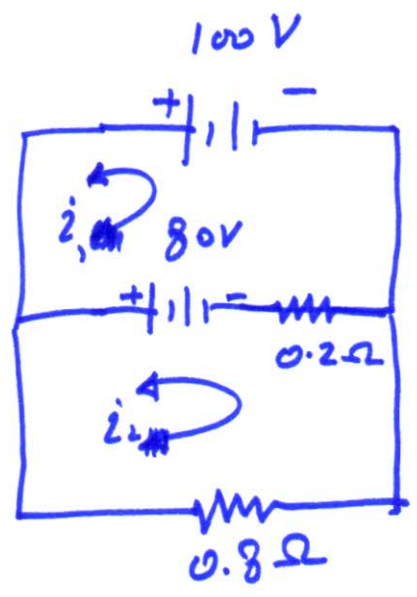
$$R_{22} = 8 + 4 = 12$$

$$R_{12} = R_{21} = -4$$

$$\begin{bmatrix} 14 & -4 \\ -4 & 12 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 20 \\ 12 \end{bmatrix}$$

$$i_1 = ? \quad i_2 = ?$$

Exp-2



$R_{11} = 0.2 \Omega$

$R_{22} = 1.0 \Omega$

$R_{12} = R_{21} = -0.2 \Omega$

$V_1 = 100 - 80 = 20V$

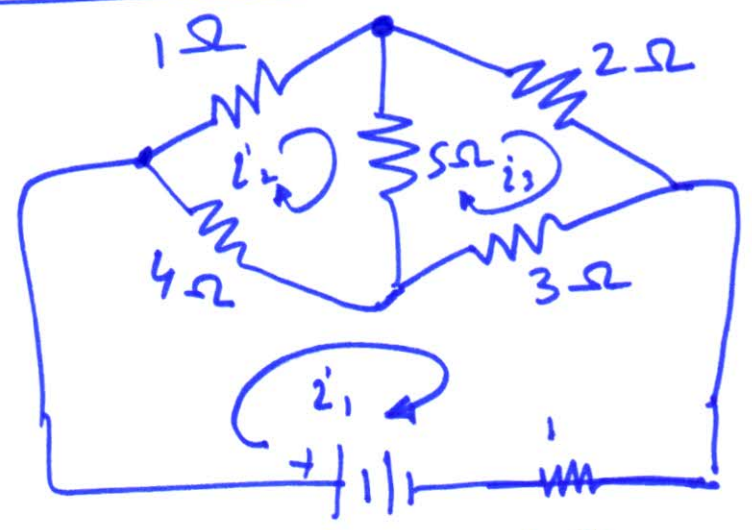
$V_2 = 80$

$$\begin{bmatrix} R_{11} & R_{12} \\ R_{21} & R_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$

$$\begin{bmatrix} 0.2 & -0.2 \\ -0.2 & 1.0 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 20 \\ 80 \end{bmatrix}$$

$i_1, i_2 = ?$

Exp-4



$R_{11} = 4 + 3 = 7 \Omega$

$R_{22} = 5 + 4 + 1 = 10 \Omega$

$R_{33} = 3 + 5 + 2 = 10 \Omega$

$R_{12} = -4 \Omega = R_{21}$

$R_{13} = R_{31} = -3$

$R_{23} = R_{32} = -5$

$V_1 = 4, V_2 = 0, V_3 = 0$

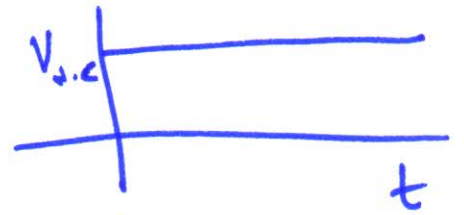
$$\begin{bmatrix} R_{11} & R_{12} & R_{13} \\ R_{21} & R_{22} & R_{23} \\ R_{31} & R_{32} & R_{33} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix} = \begin{bmatrix} 4 \\ 0 \\ 0 \end{bmatrix}$$



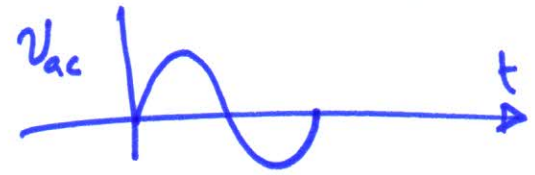
# Complex Circuit Analysis

(2) (35)

D.C  $\rightarrow$  Direct current



A.C  $\rightarrow$  Alternating current



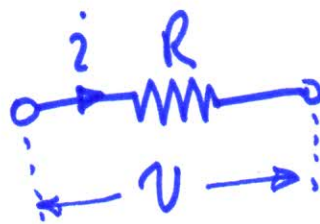
frequency of D.C,  $f = 0$

frequency of A.C,  $f = 50 \text{ Hz (cps)}$   
 $= 60 \text{ Hz (America)}$

Three basic element in power system

① Resistor, ② Inductor ③ Capacitor.

① Resistor



$$P = i^2 \cdot R$$

$$P = V i$$

ohm's Law

$$V = i R$$

$$i = V/R$$

$$R = \text{ohms}$$

D.C/A.C

$$P = V i \cos \phi$$

$\phi =$  Angle between  $V/i$  is zero

$$\cos \phi = \cos 0 = 1.0$$

$$P = V i$$

No Energy is stored in Resistor. ② (36)  
 All Energy is Consumed in Resistor.

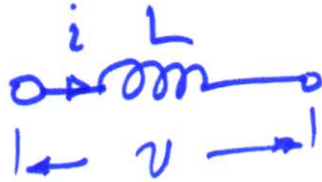
$$E = i^2 \cdot R \cdot t$$

Instantaneously change  
 Voltage changes the  
 instantaneous  
 change in  
 Current.



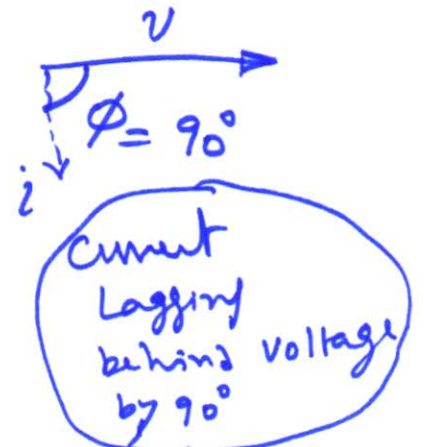
$$P = Vi$$

## ② Inductor



Normally used for motor

$$V = L \frac{di}{dt}$$



Original formulae: Faradays law

$$V = \frac{d\psi}{dt}$$

$$\psi = \text{flux linkages} = Li$$

$$V = \frac{d(Li)}{dt} = L \frac{di}{dt} + i \frac{dL}{dt}$$

$$V = L \frac{di}{dt}$$

(if  $L = \text{Constant}$ , which is normally the case)

$$X_L = 2\pi fL$$

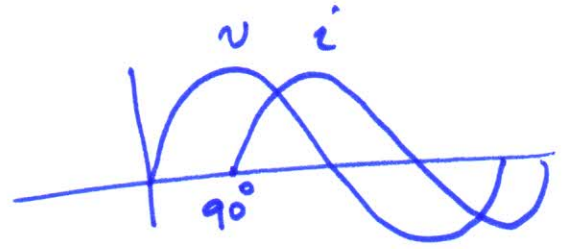
(Inductive reactance)  
in ohms  $\Omega$

$$X_L = 0$$

D.C

$$X_L = 2\pi fL$$

A.C



Current does not  
change instantaneously  
Always a delay in  
inductive circuit

Energy is stored in  
inductor.

$$V_L = L \frac{di}{dt}$$

$$P = V_L \cdot i$$

$$dW = P \cdot dt$$

$$dW = V_L \cdot i \cdot dt \\ = L \frac{di}{dt} \cdot i \cdot dt$$

$$dW = L i di$$

$$W = L \int_0^I i \cdot di = \frac{1}{2} L I^2$$

Energy consumed is  
ideally zero.

Practically yes, but  
negligibly small



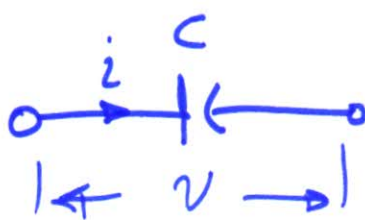
$$W = \frac{1}{2} L I^2$$



# Capacitor

(2) (38)

$$i = C \frac{dv}{dt}$$



original formulae  $\Rightarrow i = \frac{dq}{dt}$

$$q = CV$$

$$i = \frac{dq}{dt} = \frac{d(CV)}{dt} = C \frac{dv}{dt} + v \frac{dC}{dt}$$

$i = C \frac{dv}{dt}$  only if  $C = \text{constant}$

$$P = vi = v \cdot \frac{dq}{dt}$$

Energy stored in  
a capacitor

~~$\frac{dW}{dt} = \frac{dP}{dt} =$~~

$$dE = P \times dt$$

$$dE = v \cdot \frac{dq}{dt} \cdot dt$$

$$dE = v \cdot dq$$

$$v = \frac{q}{C}$$

$$dE = \frac{q}{C} \cdot dq$$

$$Q = CV$$

$$v = \frac{Q}{C}$$

$$\Rightarrow E = \frac{1}{C} \int_0^Q q \cdot dq$$

$$E = \frac{1}{C} q^2 / 0^2$$

$$E = \frac{Q^2}{2C}$$

As  $Q = CV$

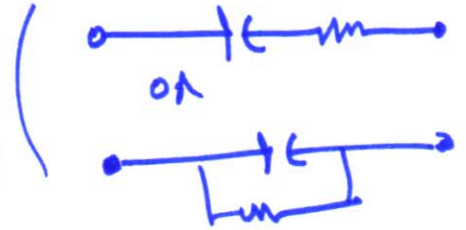
hence

$$E = \frac{1}{2} CV^2$$

No Energy is consumed in a (ideal) capacitor

However in a real capacitor only small energy is consumed.

Actual model of capacitor



AC/DC

$$P = vi \cos \phi$$



$$P = vi \times 0$$

$$P = 0$$

$$\phi = 90^\circ$$

current is leading by  $90^\circ$

$$X_c = \frac{1}{2\pi fC}$$

$f = 0$  for D.C

$X_c = \infty$  (open circuit)  $\Omega$

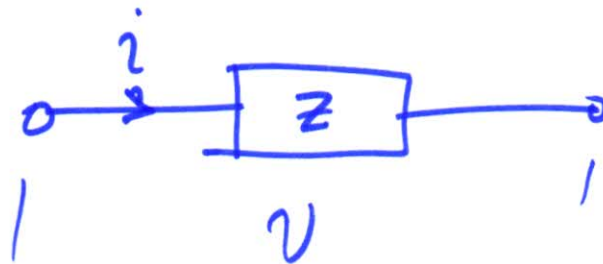
$X_c = \frac{1}{2\pi fC}$  (A.C, Capacitive reactance)

units are ohm

# Complex circuit

(240)

Impedance (Combined affect of R, L, C to oppose Electric current is called impedance)  
Combination of R, L and C is called a Complex circuit.



$$V = iZ$$



$R = \text{ohms (Resistor)} \Omega$

$L = \text{Inductance inductance in Henry (H)}$

$C = \text{Capacitance in Farads (F)}$

$R \rightarrow \Omega, m\Omega, M\Omega, k\Omega$

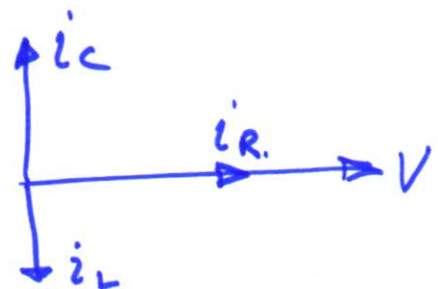
$L \rightarrow H, mH$

$C \rightarrow F, \mu F, nF, pF$

$R = \text{ohms}$

$X_L = 2\pi fL$  (ohms)

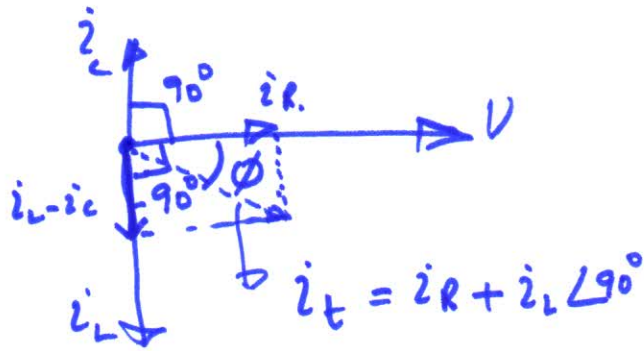
$X_C = \frac{1}{2\pi fC}$





$$Z = R + jX_L - jX_C$$

$$j = 1 \angle 90^\circ$$



$$\phi = \tan^{-1} \left( \frac{X_L - X_C}{R} \right)$$

$$\cos \phi = \text{Power Factor}$$

$\phi$  is the angle between  $V$  and  $i$

→ if  $X_L > X_C$ , the net reactance will be inductive

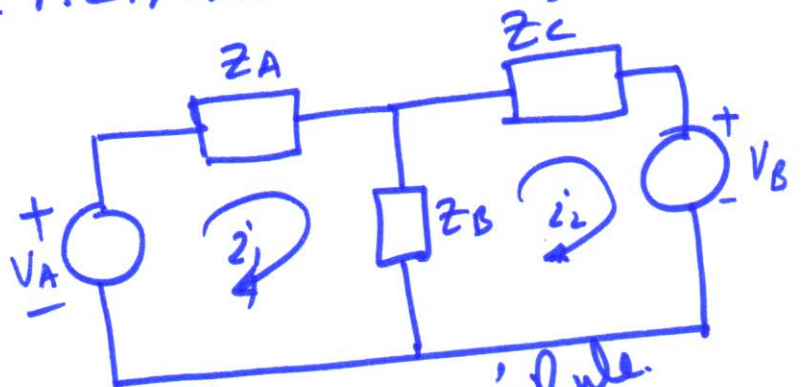
→ if  $X_C > X_L$  then the net reactance will be capacitive.

$R \rightarrow$  Resistance  
 $Z \rightarrow$  Impedance

$$\frac{1}{R} = G = \text{Conductance } (\sigma) \text{ (mho)}$$

$$\frac{1}{Z} = Y = \text{Admittance } (\sigma) \text{ (mho)}$$

$$\begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} V_1 \\ V_2 \end{bmatrix}$$



Cramer's Rule.

$$\left. \begin{aligned} Z_{11} &= Z_A + Z_B \\ Z_{22} &= Z_B + Z_C \\ Z_{12} &= Z_{21} = -Z_B \end{aligned} \right\} \begin{aligned} V_1 &= V_A \\ V_2 &= -V_B \end{aligned}$$